PHYSICS 521 - FALL 2010 Midterm Exam II

Problem 1

A particle of mass m and charge q is moving in the *x*-direction under the influence of a uniform electric field $\vec{E} = \mathcal{E}_0 \hat{x}$.

Calculate the average acceleration

$$\frac{d^2 \langle X \rangle}{dt^2}$$

and compare your result with the one expected from classical mechanics.

Problem 2

A spin-1/2 particle of magnetic moment $\vec{\mu} = \gamma \vec{S}$, where

$$S_x = \frac{\hbar}{2} \begin{pmatrix} 0 & 1\\ 1 & 0 \end{pmatrix} , \quad S_y = \frac{\hbar}{2} \begin{pmatrix} 0 & -i\\ i & 0 \end{pmatrix} , \quad S_z = \frac{\hbar}{2} \begin{pmatrix} 1 & 0\\ 0 & -1 \end{pmatrix}$$

is placed in a uniform magnetic field

$$\vec{B} = B_0 \left(\begin{array}{c} 0\\ 3/5\\ 4/5 \end{array} \right)$$

At t = 0 the *z* component of its spin is measured and found to be $+\hbar/2$.

If the *x* component of the spin is measured at time t > 0, what are the possible outcomes and with what probability will each occur?