

# PHYSICS 231 – TEST # 3

NAME:

STUDENT ID #:

## USEFUL CONSTANTS

$$\begin{aligned}\epsilon_0 &= 8.85 \times 10^{-12} \text{C}^2/(\text{N} \cdot \text{m}^2) \\ k &= \frac{1}{4\pi\epsilon_0} = 8.988 \times 10^9 \text{N} \cdot \text{m}^2/\text{C}^2 \\ e &= 1.6 \times 10^{-19} \text{C} \\ m_e &= 9.1 \times 10^{-31} \text{kg} \\ \mu_0 &= 4\pi \times 10^{-7} \text{T} \cdot \text{m}/\text{A} \\ g &= 9.81 \text{N}/\text{kg}\end{aligned}$$

## USEFUL FORMULAS

Magnetic force

on point charge:  $\vec{F} = q\vec{v} \times \vec{B}$

on wire:  $\vec{F} = I \int d\vec{l} \times \vec{B}$

Magnetic flux through closed surface:

$$\Phi_B = \int \vec{B} \cdot d\vec{A} = 0$$

In a constant magnetic field a particle moves on circle of radius

$$R = \frac{mv}{|q|B}$$

Current loop:

force:  $\vec{F} = \vec{0}$ .

torque:  $\vec{\tau} = \vec{\mu} \times \vec{B}$ ,  $\vec{\mu} = I\vec{A}$ .

energy:  $U = -\vec{\mu} \cdot \vec{B}$ .

Magnetic field

due to point charge:

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \vec{r}}{r^3}$$

due to wire (**Biot-Savart law**):

$$\vec{B} = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{l} \times \vec{r}}{r^3}$$

Ampère's law:

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{enc}$$

outside infinite straight wire:

$$B = \frac{\mu_0 I}{2\pi r}$$

on axis of circular wire of radius  $a$ :

$$B_x = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}$$

at center of  $N$  circular loops:

$$B_x = \frac{\mu_0 N I}{2a}$$

inside solenoid of  $n$  turns per unit length:

$$B = \mu_0 n I$$

Emf

in closed loop (**Faraday's law**):

$$\mathcal{E} = \oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$$

in moving loop:

$$\mathcal{E} = \oint (\vec{v} \times \vec{B}) \cdot d\vec{l}$$

wire of length  $L$  in uniform  $\vec{B} \perp \vec{L} \perp \vec{v}$ ,

$$\mathcal{E} = vBL$$